

C.C.M.A.C. – 2<sup>nd</sup> Meeting – December 5, 2013

**COMMON CORE  
MATHEMATICS ADVISORY  
COMMITTEE**

# CCMAC – GOALS

## By Priority

### Elementary

Research and create new assessments that align with planned Common Core assessments

### Secondary

Recommend a Secondary Math Pathway for the District

**Identify Necessary Instructional Shifts**

**Identify Necessary Types of Technology Tools**

**Write a Common Core Math Transition Plan**

# Recommend a Secondary Math Pathway

## Traditional vs. Integrated

### ⦿ Recommendation Based On

- Research of CC Math Standards
- Alignment to SMPs and Best Practices
- Alignment to SBAC Assessments

**Agenda Change**

Discussing Curriculum First

## Acceleration Pathways

### ⦿ Acceleration Points

- Middle School
- High School

### ⦿ Acceleration Type

- Double Up (2:1)
- Accelerated (3:2)
- Enhanced (4:3)
- Other

# Integrated and Traditional Pathways

## The History

### Traditional Pathway:

- Algebra/Geometry/Algebra sequence evolved in the 1800s one course at a time as U.S. universities (esp. Ivy League) increased their **admission requirements** year by year.



### Integrated Pathway:

- Reform movement under Felix Klein in the early 1900s. It was designed so students received a curriculum unified under math **function**, not math **subject**.
  - Accepted by almost every nation except the United States



# Integrated vs. Traditional Pathways

## Current Pre-Conceptions/Stereotypes

### Traditional – Common in U.S. (Grade 8-11)

- **Content**: Sequential – Algebra → Geometry → Algebra 2
- **Practice**: Direct instruction in class, followed by practice at home. Students might not apply this math to real-world circumstances.
  - **Assessed products**: Single day tests or worksheet assignments, completed individually.

### Integrated – Common Internationally (all Grades) and in U.S. Grades K-7

- **Content**: Integrated – Algebra/Geometry/Statistics
- **Practice**: No direct instruction, instead focusing on “discovery” style lessons to teach concepts. Students might practice at home with no direct instruction on a topic.
  - **Assessed products**: Multiple day lab-type projects completed in groups.

# Integrated vs. Traditional Pathways

## What's in a Name?

Traditional – **Content** and **Practice** Standards Changed Substantially

- The Traditional Pathway is not very “traditional.”

Integrated – Now Shares SMPs With Traditional Pathway

- Integrated must now be judged on the value of its **Content**, not its **Practices**



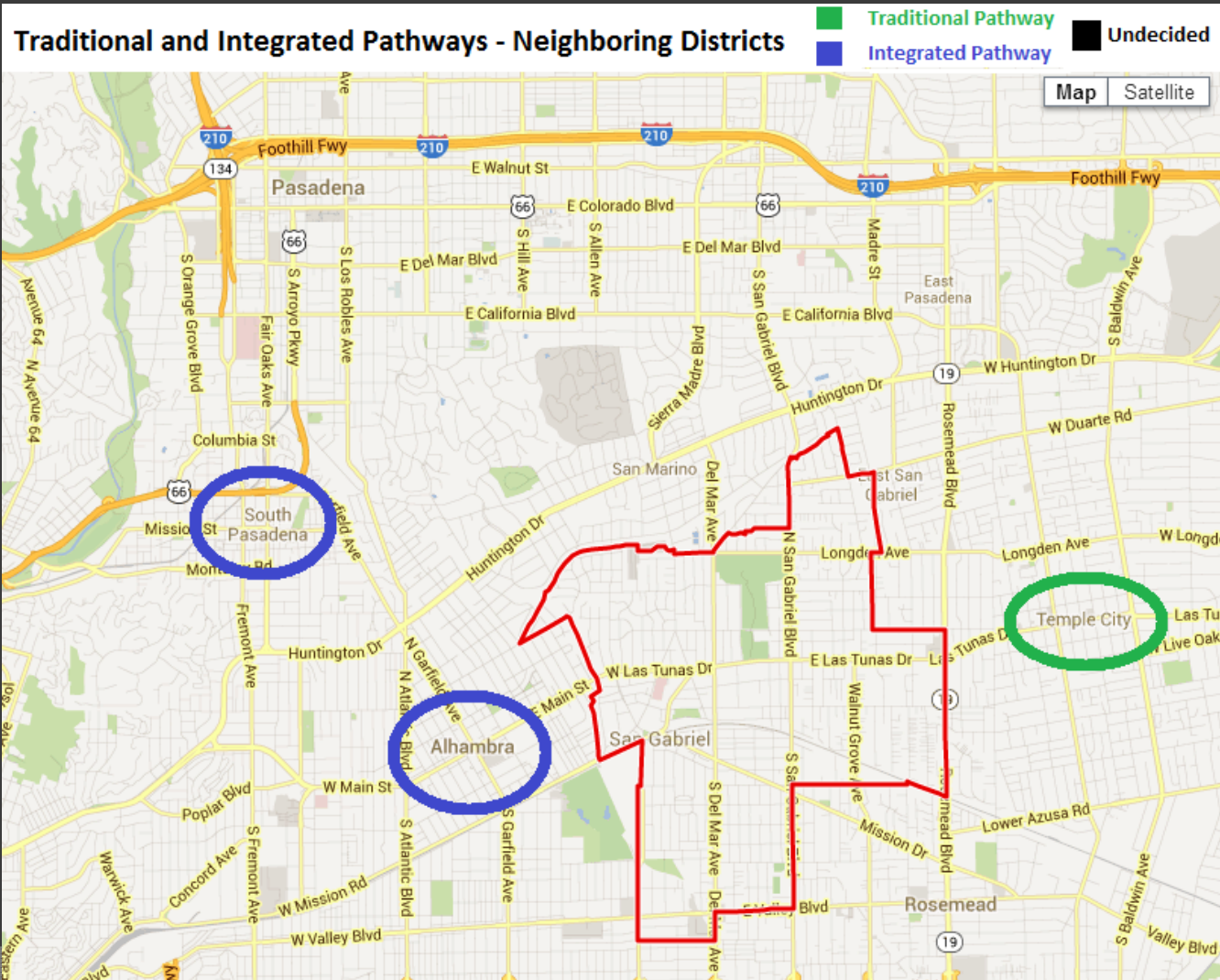
**“You must unlearn what you have learned.”**

**-Yoda**



# Integrated vs. Traditional Pathways

## What Are Other Districts Choosing?



### Integrated

Alhambra USD  
Charter Oak USD  
Covina-Valley USD  
Duarte USD  
El Monte Union High SD  
Norwalk-La Mirada USD  
Oceanside USD  
Perris Union High SD  
San Diego USD  
Shasta County (35 Districts)  
South Pasadena USD

### Traditional

Bonita USD  
Santa Monica-Malibu USD  
Walnut Valley USD  
Whittier Union High SD  
La Canada USD

### Undecided

Baldwin Park USD  
Claremont USD  
Chaffey Joint Union High SD  
Glendora USD  
Monrovia USD

# Integrated vs. Traditional Pathways

## Why Are Districts Choosing the Integrated Pathway?

### Curriculum and Implementation Effects on High School Students' Mathematics Learning From Curricula Representing Subject-Specific and Integrated Content Organizations

Douglas A. Grouws, James E. Tarr, Óscar Chávez,  
Ruthmae Sears, Victor M. Soria, and Rukiye D. Taylan  
*University of Missouri*

This study examined the effect of 2 types of mathematics content organization on high school students' mathematics learning while taking account of curriculum implementation and student prior achievement. The study involved 2,161 students in 10 schools in 5 states. Within each school, approximately 1/2 of the students studied from an integrated curriculum (Course 1) and 1/2 studied from a subject-specific curriculum (Algebra 1). Hierarchical linear modeling with 3 levels showed that students who studied from the integrated curriculum were significantly advantaged over students who studied from a subject-specific curriculum on 3 end-of-year outcome measures: Test of Common Objectives, Problem Solving and Reasoning Test, and a standardized achievement test. Opportunity to learn and teaching experience were significant moderating factors.

*Key words:* Curriculum; Curriculum effectiveness; HLM, Integrated curriculum; Secondary mathematics

#### Traditional Math Integrated Math

##### Traditional Organized Pathway

- Objectives built into subject-specific content
- Taught via rules, procedures
- Lecture based, teacher-centered
- Continuous practice

##### Integrated Organized Pathway

- Objectives from algebra, geometry, functions, statistics interwoven
- Real world problems and experiences
- Teacher serves as facilitator and coach
- Collaborative learning
- Practice with a purpose

#### Why Do They Differ?

##### INTEGRATED

- ❖ Objectives from algebra, geometry, functions, math modeling, and probability and statistics, are interwoven
- ❖ Real world problems are investigated via lab-type experiences
- ❖ Teacher serves as facilitator and coach
- ❖ Collaborative learning
- ❖ Practice with a purpose



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# Integrated vs. Traditional Pathways

## Common Core Practices

Both Integrated and Traditional pathways are governed by the same **practices** – the **Standards of Mathematical Practice**

**1** *Make sense of problems and persevere in solving them.*



**2** *Reason abstractly and quantitatively.*



**3** *Construct viable arguments and critique the reasoning of others.*



**4** *Model with mathematics.*



**5** *Use appropriate tools strategically.*



**6** *Attend to precision.*



**7** *Look for and make use of structure.*



**8** *Look for and express regularity in repeated reasoning.*



# Integrated vs. Traditional Pathways

## Common Core Content

### 1997 Algebra, Geometry, Algebra II Crosswalk

- Review the “**CCSS Crosswalk – 1997 – Simplified**” handout.
- You can also look at the longer “**CCSS Crosswalk - 1997.**” To delve deeper into each standard.

**Discuss (4 songs):**

**What differences and similarities to the 1997 Content Standards do you see?**

**What does this mean for your site?**

Green = Expanded

Black = Relatively Unchanged

Brown = Partial

Red = Not Part of This CCSS Content Area

#### Algebra I Standards

1.0 Students identify and use the arithmetic properties of subsets of integers and rational, irrational, and real numbers, including closure properties for the four basic arithmetic operations where applicable.

1.1 Students use properties of numbers to demonstrate whether assertions are true or false.

2.0 Students understand and use such operations as taking the opposite, finding the reciprocal, taking a root, and raising to a fractional power. They understand and use the rules of exponents.

3.0 Students solve equations and inequalities involving absolute values.

4.0 Students simplify expressions before solving linear equations and inequalities in one variable, such as  $3(2x-5) + 4(x-2) = 12$ .

# Acceleration Pathways

## A New Necessity

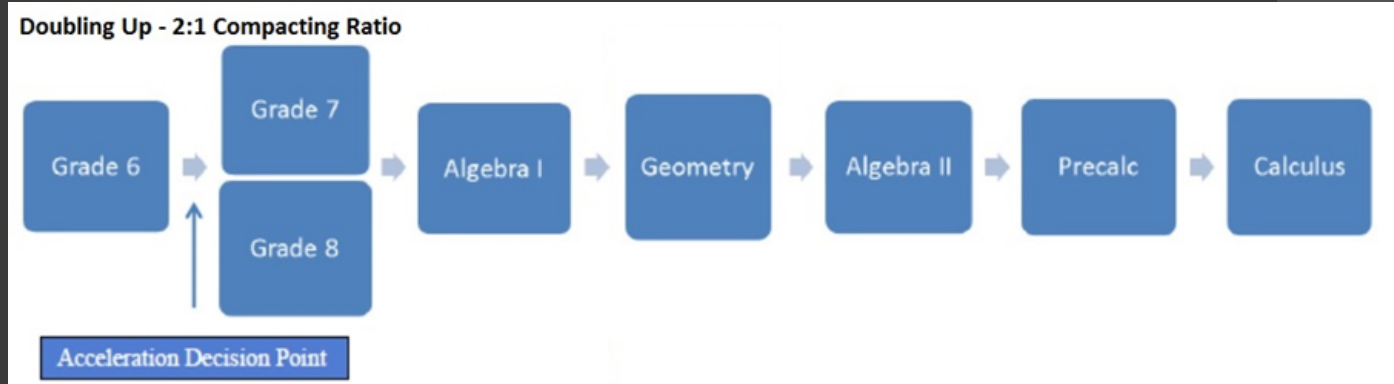
- ◎ The Common Core Math standards no longer repeat between grade levels.
  - Material is consistently expanded upon, not repeated.
- ◎ 7<sup>th</sup> → 8<sup>th</sup> Grade Progression Examples
  - Create Single Variable Equations and Inequalities →
    - Graphing and Solving 1-Variable Linear Equations
  - Proportionality and Unit Rate →
    - Graph and Interpret Proportional Relationships
  - Random Sampling and Basic Probability →
    - Create and Investigate Scatterplots from Experimental Data
    - Identify Positive, Negative, Linear Associations, and Estimate Line of Best Fit – Interpret Slope and Y-Intercept
- ◎ In light of this, current practice needs to be revisited



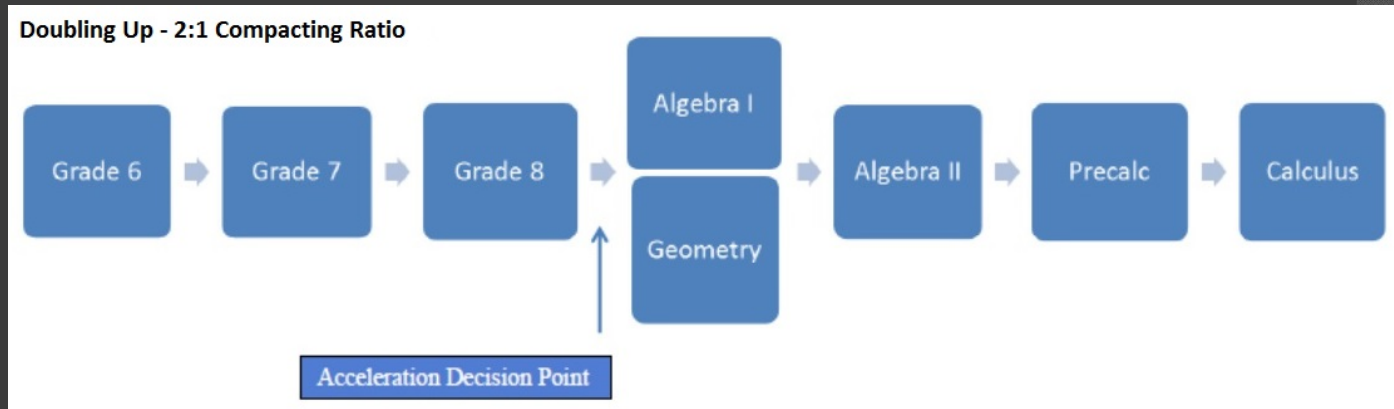
# Acceleration Pathways

## “Doubling Up”

JMS  
Acceleration



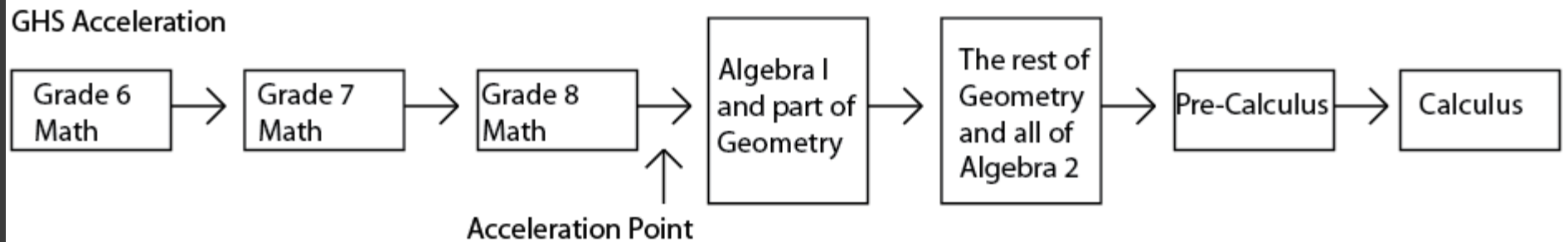
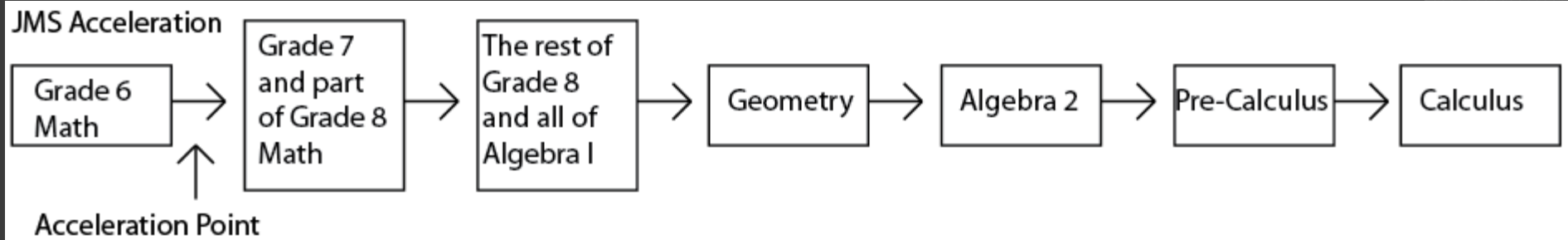
GHS  
Acceleration



Two math courses taken simultaneously

# Acceleration Pathways

## “Accelerated Pathway” – 3:2 Ratio

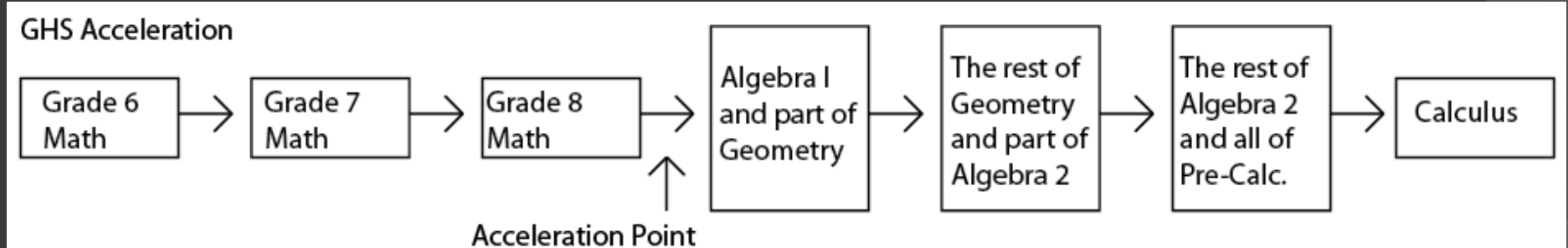
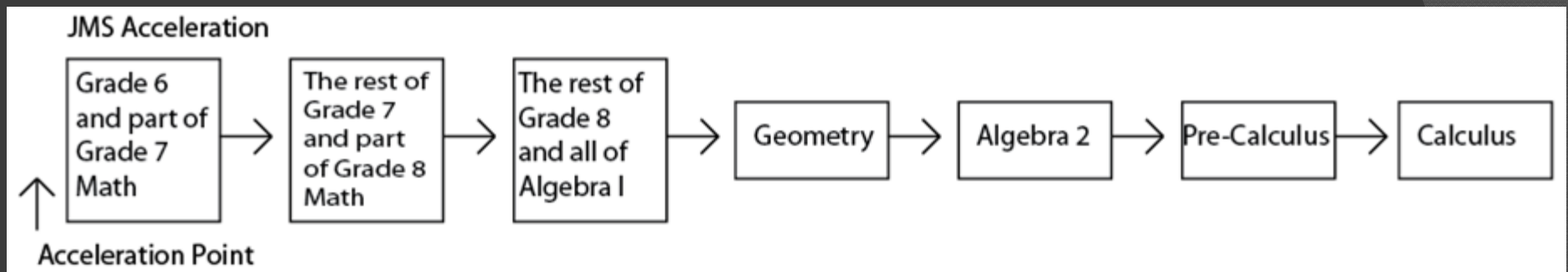


Can occur at any grade where a student will remain on site for two years

- 6<sup>th</sup>, 7<sup>th</sup>, 9<sup>th</sup>, 10<sup>th</sup>, 11<sup>th</sup> Grades

# Acceleration Pathways

## “Enhanced Pathway” – 4:3 Ratio



Acceleration point can occur in 6<sup>th</sup>, 9<sup>th</sup>, and 10<sup>th</sup> Grades

- Student would have to remain at that school site for three years

# Acceleration Pathways

## Other Options

### Summer

- Students could take a course of math over the summer to advance.
- Makes scheduling easier – no compacted courses
- Paid course – Accessibility Problem

### No Acceleration Pathway

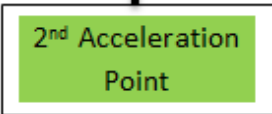
- Offer enrichment and differentiation through honors coursework



# Common Core Acceleration Examples

## The New “Grade Level”

	8 <sup>th</sup> Grade	9 <sup>th</sup> Grade	10 <sup>th</sup> Grade	11 <sup>th</sup> Grade	12 <sup>th</sup> Grade
Grade Level	8 <sup>th</sup> Grade Math	Algebra I	Geometry	Algebra II	Pre-Calculus
Accelerated Once – JMS	8 <sup>th</sup> Grade Math/ Algebra I	Geometry	Algebra II	Pre-Calculus	Calculus AP Calculus AB
Accelerated Twice	8 <sup>th</sup> Grade Math/ Algebra I	Geometry/ Algebra II	Algebra II/ Pre-Calculus	Calculus AP Calculus AB	AP Calculus BC


Note – Acceleration Assumes 3:2 Ratio